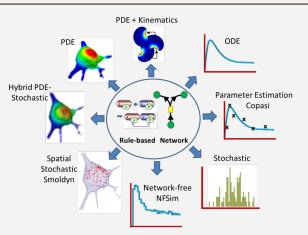


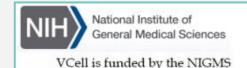
A modeling environment for the simulation of cellular events. Download at <u>vcell.org</u> Version 7.7 July 2025



Constructive Solid Geometry: Dendritic Spine



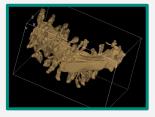
Virtual Cell is developed by the Center for Cell Analysis and Modeling at the University of Connecticut Health Center. It is funded by the National Institute of General Medical Sciences (NIGMS)





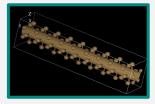
Dendritic Spine CSG Introduction

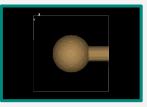
Dendritic spines are small membrane protrusions from a neuron's dendrite that aid in the transduction of electrical signals between nerve cells. To the top right is a VCell representation of a dendrite based on z-stack of microscopy images (see <u>Tutorial for Image Based Geometry</u>) The model is described in Brown wt al., 2008 <u>https://vcell.org/brown-et-al-2008</u>



To develop faster and more understandable simulations, it is better to start with an artificial geometry where all effects are clearly seen. In the middle right is a **Constructive Solid Geometry** (CSG) model of a dendrite.

In this tutorial, we will focus on creating a model of one dendritic spine (see bottom right), which consists of a bouton (a sphere with a radius 0.5 um) on a dendritic stem (a cylinder with a length of 0.5 um and a diameter of 0.4 um). We will simulate it in a 3D space that is $2 \times 2 \times 2$ um.





Constructive Solid Geometry: Dendritic Spine

Objective:

Create a single Biomodel of a dendritic spine using Constructive Solid Geometry (CSG) in Virtual Cell modeling and analysis software.

Goals:

- → Learn basic CSG concepts, such as defining solid bodies, scaling, translation and union.
- → Run a simulation to verify accuracy of your model.

General familiarity with VCell software is recommended. Although this tutorial can be followed by a VCell novice, it is recommended that novice users first look through the VCell tutorials available at https://vcell.org/support

Model building can be matched to the BioModel **Tutorial_CSG_DendriticSpine** in the **Tutorial folder** in the **VCell Database**.

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- 2. Creating the Bouton (Sphere)
 - 2.1 Define the Bouton of the Spine
 - 2.2 Scale Sphere to the Proper Size
 - 2.3 Move Sphere to the Desired Position
- 3. Creating the Neck (Cylinder)
 - 3.1 Define the Neck of the Spine
 - 3.2 Scale Cylinder to the Proper Size
 - 3.3 Move Cylinder to the Desired Position
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 - 3.5 Verifying the Model's Dimensions

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- 4. Testing the Model via Diffusion Simulation
 - 4.1 Set up Model Physiology
 - 4.2 Link Model Physiology to Geometry
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 - 4.6 Viewing Volume Simulation
 - 4.7 Viewing Membrane Simulation



Name	Value
subdomain1	Constructed Solid Geometry
subdomain0	Constructed Solid Geometry

Starting Constructive Solid Geometry

1.1 Create Application and Geometry

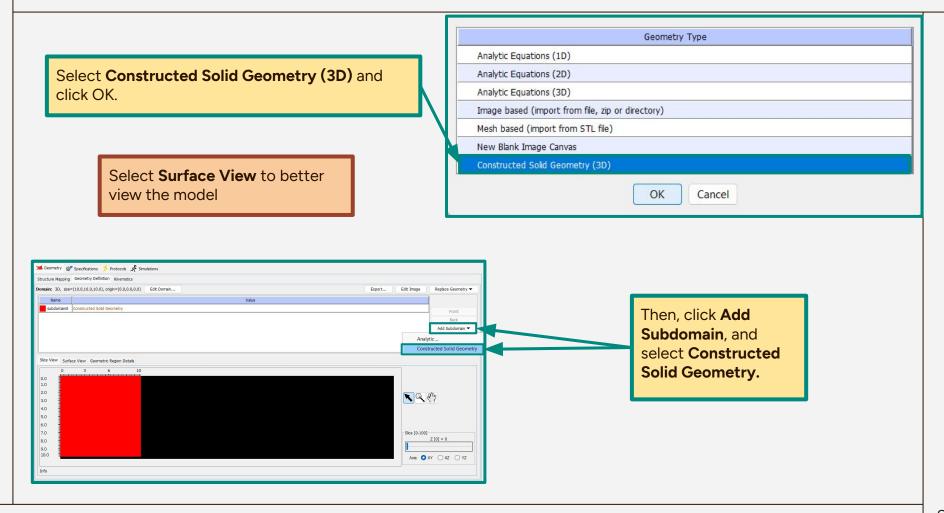
Select Application. Right click, then select New Application → Deterministic.

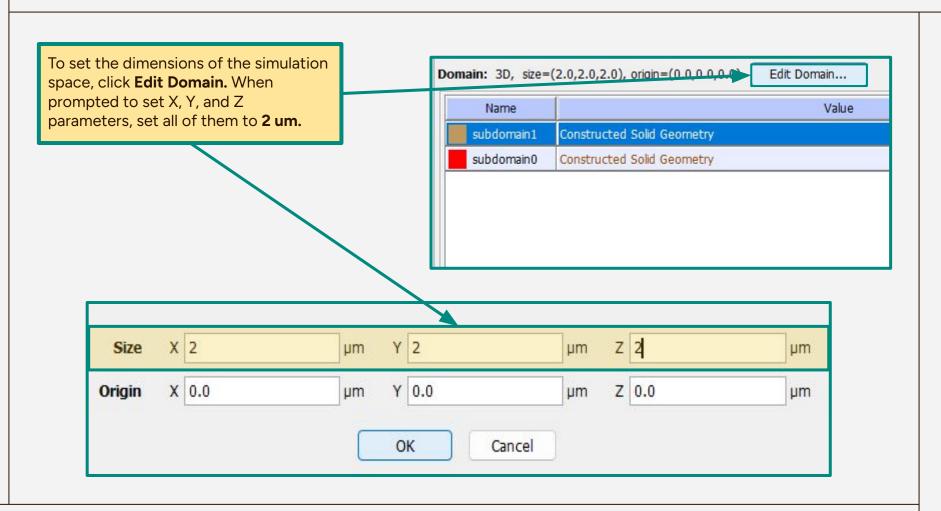
Application subsection.

Make sure to select Geometry under the

Click Add Geometry and select New.

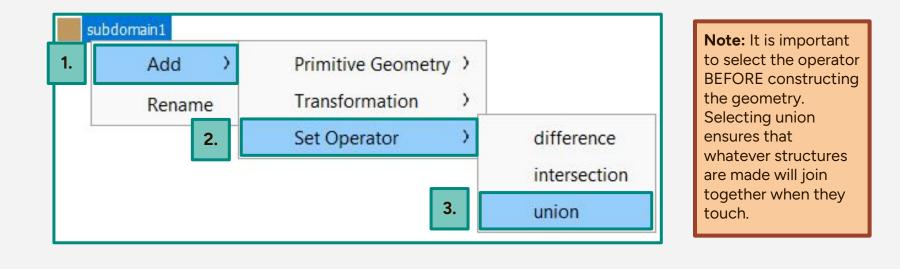
BioModel4 Physiology * Reaction Diagram Reactions (0) Structures (1) D Species (0) Molecules (0) Observables (0) BioModel4 🗯 Geometry 💣 Specifications 🔸 Protocols 📌 Simulations Parameter Estimation Physiology New Application > Deterministi Para Structure Mapping Geometry Definition Kinematics 🐉 Reaction Diagram Patt Expand All Stochastic Reactions (0) Domain: 0D, compartmental Edit Domain. Add Geometry -Network-Free Collapse All Structures (1) Name Value New. D Species (0) Compartment Open from. Molecules (0) Observables (0) Applications (1) d/de Application0 Geometr Specifications A. Protocols VCel DB BMDB Pathway Comm A Simulations BioModels MathModels Geometries E Search C Parameter Estimation Biological Models Parameters, Functions, Units, etc 🗄 🎇 My BioModels (SreeKola) (4) Pathway Shared With Me (2) Tutorials (10) Add Subdomain 🔻 Public BioModek (1017) Delete Published (220) - Curated (55) H G Uncurated (742) ... VCell DB BMDB Pathway Comm BioModels MathModels Geometries E Search Biological Models 🚯 🧱 My BioModels (SreeKola) (4) E _ Shared With Me (2) E D Tutorials (10) Public BioModels (1017)

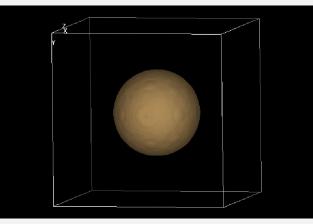




1.2 Select Appropriate Framework

Right click the subdomain, select Add, navigate to Set Operator, then select Union.







Creating the Bouton (Sphere)

The construction of the dendritic spine will start by first creating a sphere that will represent the bouton (bulbous part of the spine).

2.1 Define the Bouton of the Spine

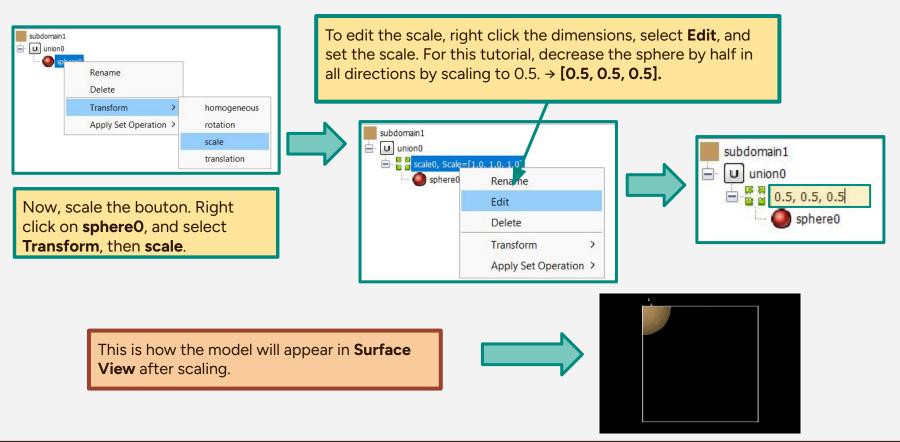
Right click Union, select Add, navigate to Primitive Geometry, then select Sphere.

nion0				11.5.10
Add	>	Primitive Geometry	>	cone
Rename		Transformation	>	cube
Delete		Set Operator	>	cylinder
Transform	>			sphere
Apply Set Operation	>			

By default, the sphere will be created in the top left corner (the point with coordinates [0,0.0] and will have the radius 1. It needs go be translated to the desired position and scaled to the proper size.

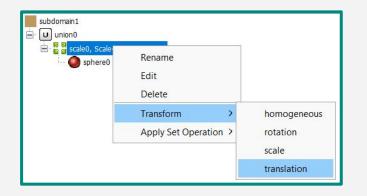


2.2 Scale Sphere to the Proper Size



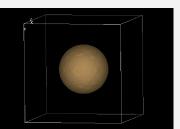
2.3 Move Sphere to the Desired Position

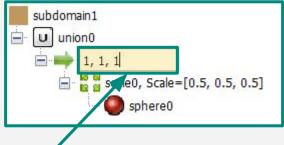
Next, translate the sphere so that it fits in the center of the simulation space. Right click on **scaleO**, select **Transform**, then **translation**.



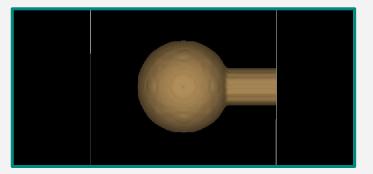
This is what the model should look in **Surface View.**







To move the center of the sphere from the point [0,0,0] to the point [1,1,1], right click the **Translation** (green arrow), click **Edit**, and set all parameters to $1. \rightarrow [1, 1, 1]$.





Creating the Neck (Cylinder)

Following the creation of the bouton, the cylindrical portion of the spine (the neck) that connects to the bouton will be created.

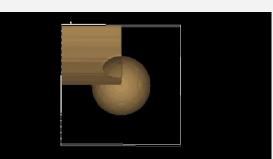
3.1 Define the Neck of the Spine

Right click on the Union operation and click Add. Select Primitive Geometry and click on Cylinder.

Add	>	Primitive Geometry	>	cone
Rename		Transformation	>	cube
 Delete		Set Operator	>	cylinder
Transform	>			sphere

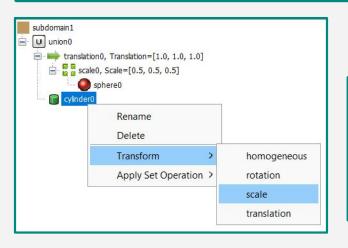
By default, the cylinder will be located in the top left corner (with coordinates [0,0,0]) and will have a radius of 1. The image shows half of the cylinder, so it needs to be scaled to the proper size and translated to the desired position.

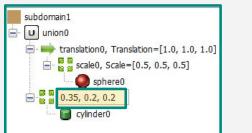




3.2 Scale Cylinder to the Proper Size

Like the bouton, the stem also needs to be scaled. Right click on **cylinder0**, and select **Transform**, then **Scale**.

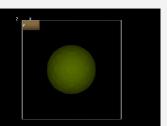




To create a cylinder of the length 0.5 and radius 0.2, it needs to be scaled to 0.25 in the length (x-direction) and 0.2 (in y and z directions). The cylinder is made longer than 0.5 to protrude inside a sphere with no holes. Note that with unions of solid bodies, protrusions do not matter. Right click on **scale1**, select **Edit**, and set the parameters to **[0.35, 0.2, 0.2]**.

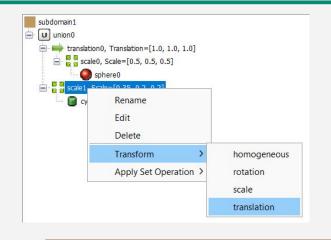
After scaling, the cylinder will remain at the coordinates [0,0,0]. To have it be correctly aligned with the sphere, it will be translated in the next slide.

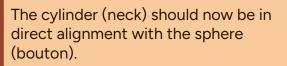


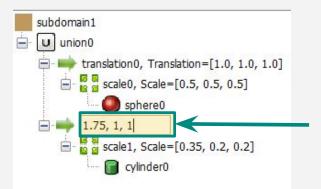


3.3 Move Cylinder to the Desired Position

To translate the cylinder so that it is directly aligned with the sphere, right click on **scale1**, select **Transform**, and then **translation**.

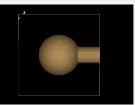


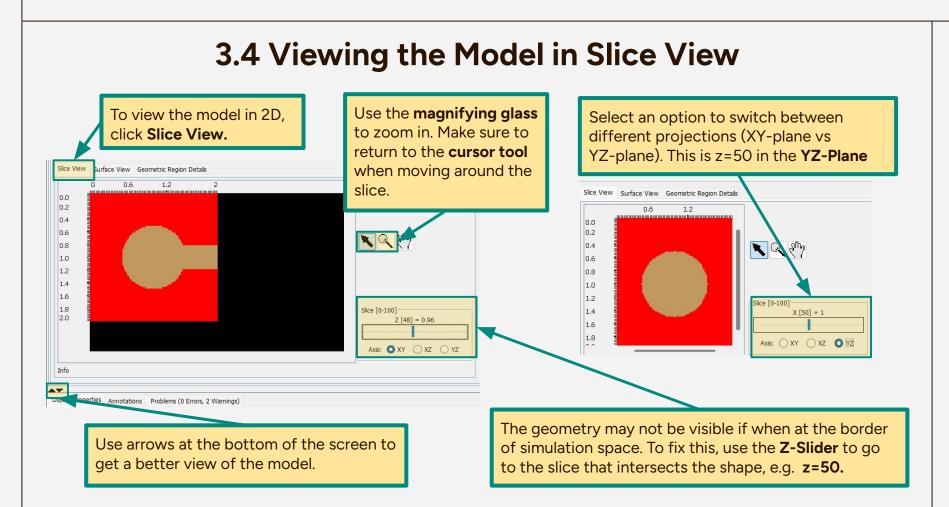




Set the translation specifications to **[1.75, 1, 1]** so that the cylinder is placed adjacent to the sphere and to the right of the simulation space.



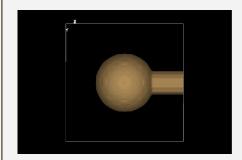




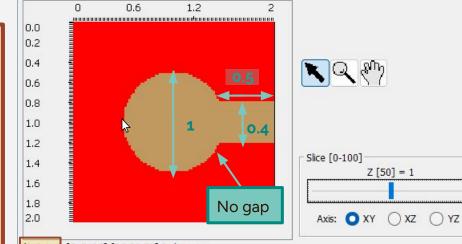
3.5 Verifying the Model's Dimensions

If done properly, the dendritic spine will have the following dimensions:

- Bouton (Sphere) Diameter = 1
- Neck (Cylinder) Diameter =0.4
- Neck (Cylinder) Height 0.5



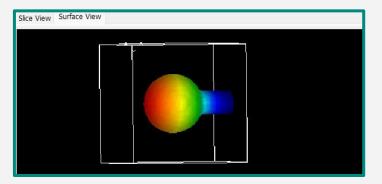
Note: Here, ensure that there are no gaps between the bouton and neck (sphere and cylinder) of the model, as this will disrupt reaction processes in during simulations.



```
(0.5,1,1) [515125] [25,50,50] Index = 1
```

Coordinates of cursor can be found here



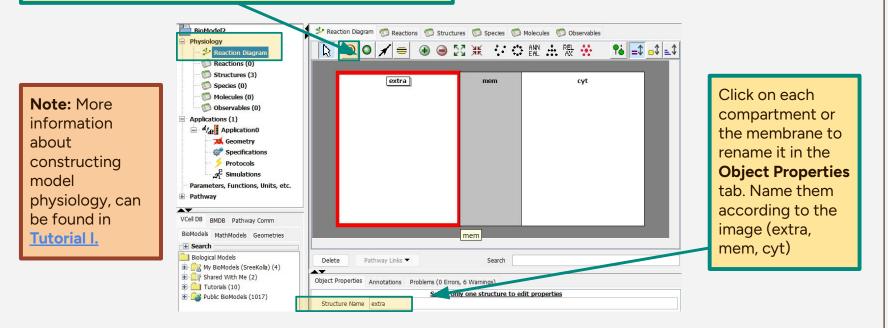


Testing the Model via Diffusion Simulation

To test if the model is functioning properly (i.e it doesn't have any holes that may leak species, touch the border, etc.), run a simulation of species diffusions in the volume and on the membrane.

4.1 Set up Model Physiology

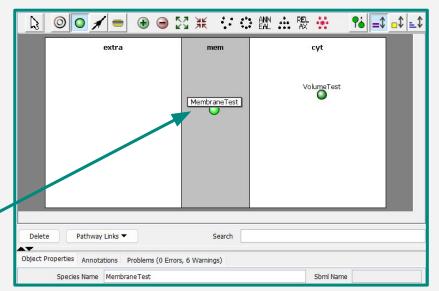
First, create a reaction diagram. Navigate to **Physiology** and under **Reaction Diagram**, create two compartments separated by one membrane.



🐓 Reaction Diagram 🏾 🌍 Reactions 🖉 Struc	ctures 🧔 Species 🧔 Molecules 🗔 Observables	
	23 💥 😳 🔅 🛍 🚠 👷 🔅	?i _1 _1 _1 _1 _1 _1
	extra mem	cyt
		VolumeTest
Delete Pathway Links 🔻	Search	
	Stal(()	
Object Properties Annotations Problems (0 Er	rors, 6 Warnings)	
Species Name VolumeTest		Sbml Name

To observe the diffusion of the species in the membrane, create a synthetic species **MembraneTest** that should be able to diffuse freely in the membrane.

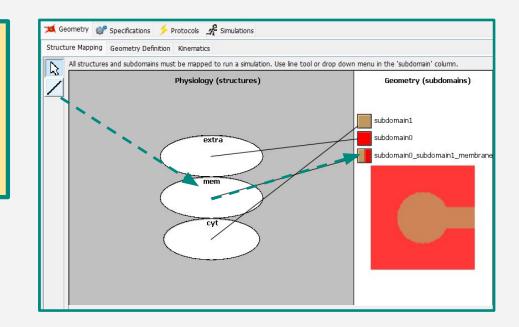
To monitor the diffusion of the species in the volume, create a synthetic species **VolumeTest** that should be able to diffuse freely within the compartment.



4.2 Link Model Physiology to Geometry

Link the compartments and membrane from the reaction diagram to subdomains to ensure that the physiology matches up with the model's geometry.

Open the **Geometry** section, and then click the **Structure Mapping** tab. Use the **Mapping Tool** to draw lines from the physiology to the appropriate geometry subdomain.



4.3 Specify Species Concentrations and Diffusions

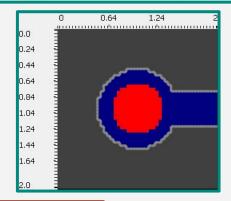
Now, set specifications for the simulation. Navigate to the **Specifications** tab, choose **Species**.

pecies Reaction	Network						
Species	Structure	Depiction 💌	Clamped	Rules	Initial Condition	Well Mixed	Diffusion Constant
VolumeTest	cyt	0			$(100.0 * ((((x - 1.0) ^ 2.0) + ((y - 1.0) ^ 2.0) + ((z - 1.0) ^ 2.0)) < 0.1)) [\mu M]$		5.0 [µm ² .s ⁻¹]
MembraneTest	mem				$(1000.0 * ((((x - 0.0) ^ 2.0) + ((y - 1.0) ^ 2.0) + ((z - 1.0) ^ 2.0)) < 0.5))$ [molecules.µm ⁻²]		1.5 [µm ² .s ⁻¹]

Initial Condition for Volume:

It is necessary to create a high concentration of a species inside the volume to monitor how the species diffuses within it. To do this, place all species, VolumeTest, within a sphere of a radius \approx 0.3162 (square root of 0.1) and center at [1, 1, 1], so it is located completely within the bouton.

 $(100.0 * ((((x - 1.0) ^ 2.0) + ((y - 1.0) ^ 2.0) + ((z - 1.0) ^ 2.0)) < 0.1))$



Diffusion Constant for Volume = 5.0

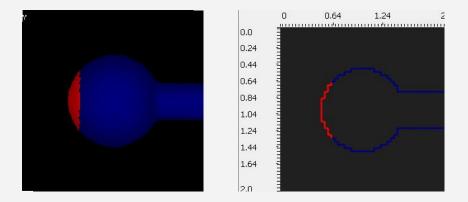
The diffusion rate is set high so that the simulation only has to run for a short period of time.

Species	Structure	Depiction 💌	Clamped	Rules	Initial Condition	Well Mixed	Diffusion Constant
VolumeTest	cyt	0			$(100.0 * ((((x - 1.0) ^ 2.0) + ((y - 1.0) ^ 2.0) + ((z - 1.0) ^ 2.0)) < 0.1)) [\mu M]$		5.0 [µm ² .s ⁻¹]
	1.000	0			$(1000.0 * ((((x - 0.0) ^ 2.0) + ((y - 1.0) ^ 2.0) + ((z - 1.0) ^ 2.0)) < 0.5))$ [molecules.µm ⁻²]		

Initial Condition for Membrane:

It is necessary to place a high concentration of a species on the membrane. To do this, create a sphere of a species, MembraneTest for this example, with a center of [0,1,1] and a radius \approx 0.7071 (square root of 0.5) so it intersects the membrane at the tip of the bouton, which is located at an x-coordinate of 0.5 in the 2x2x2 space.

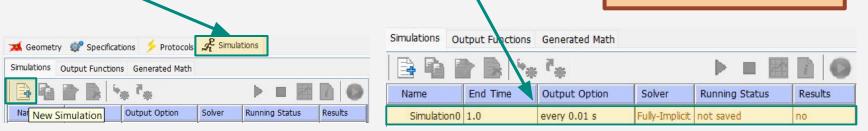
(1000.0 * ((((x - 0.0) ^ 2.0) + ((y - 1.0) ^ 2.0) + ((z - 1.0) ^ 2.0)) < 0.5))

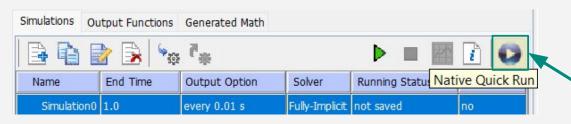


Diffusion Constant for MembraneTest = 1.5

4.4 Start the Simulation

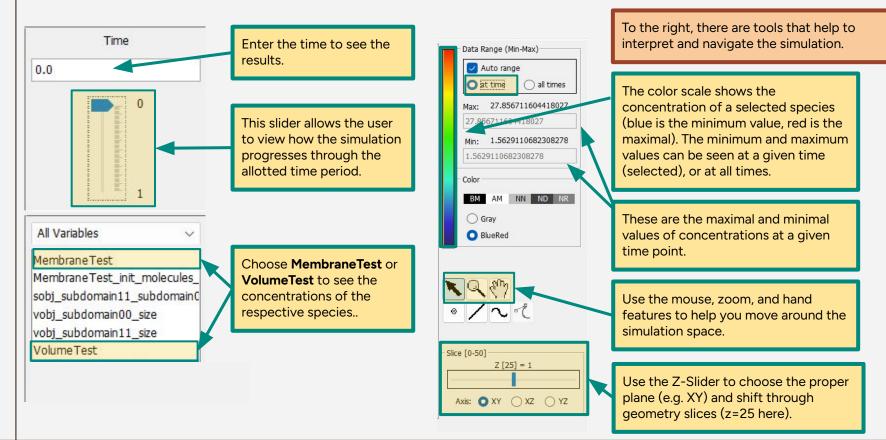
Navigate to the **Simulations** tab and click **New Simulation**. Input a small **End Time**, for example, 1.0 seconds. Set your **Output Option** to every 0.01 seconds to get 100 timepoints of the simulation's progress. **Tip:** Start the simulation with a short end time to ensure the running device can load the simulation.

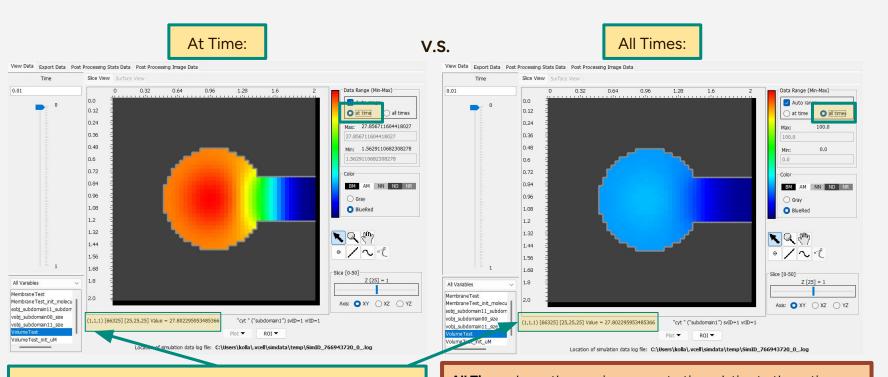




VCell can enable reactions in two ways. For this tutorial, click the blue button, **Native Quick Run**. This is preferred for quick simulations. For longer simulations, select the green button, which will run it in the VCell server.

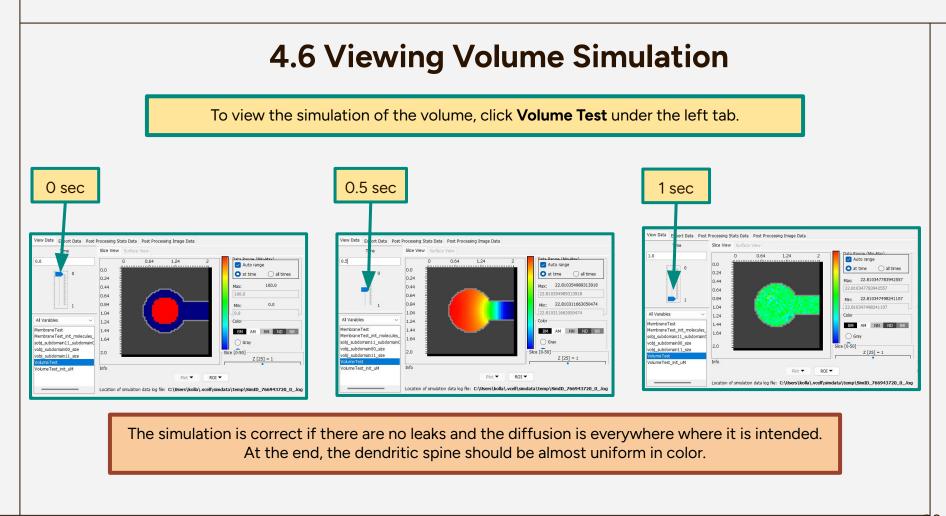
4.5 Navigating the Simulation



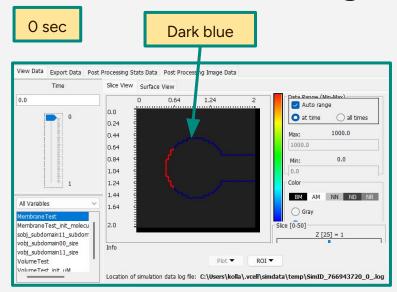


The concentration value at the cursor position [1,1,1] is 27

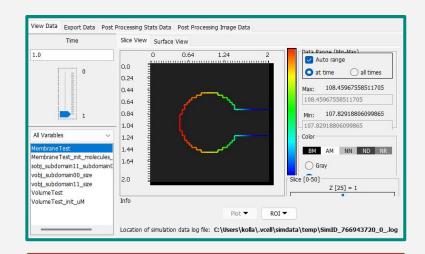
At Time shows the color scale relative to a specific time point, meaning that the red corresponds to the maximum concentration at that time and the blue represents the minimum. **All Times** shows the species concentration relative to the entire duration of the simulation. In the color scale, the red would correspond to the highest concentration of a selected species over the entire simulation, whereas the blue corresponds to the lowest. One can see that at this time point, all concentrations are relatively low compared to the maximum value 100.



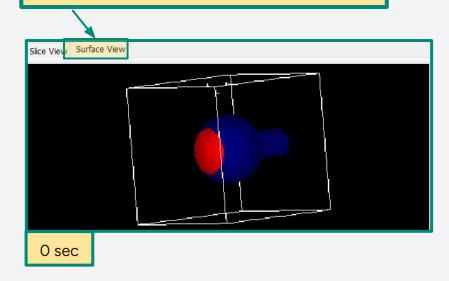
4.7 Viewing Membrane Simulation

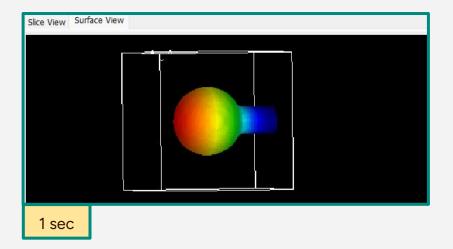


MembraneTest species is initially concentrated at the top of the bouton (the red value is 1,000), whereas the rest of the membrane has zero concentration (dark blue). 1 sec



At 1 second, the species diffuses towards the neck. For the fast diffusion, the red value at the top is 108, while the blue value at the bottom of the neck is 107, which signifies that it is almost uniform. To view the same simulation of membrane diffusion but in 3D, click on **Surface View.**





Don't forget to save your model!

Acknowledgments

This tutorial was prepared by Sreekirthana Kolla (East Granby High School) and Justine Laureano (East Hartford High School) under the guidance of Dr. Michael L. Blinov, Associate Professor, Center for Cell Analysis and Modeling. The students were funded by the Department of Health Career Opportunity Programs; the Aetna Foundation; Connecticut State Legislative Fund; John and Valerie Rowe Health Professions Scholars Program; The Hartford; the University of Connecticut Foundation; the Friends of the Department of Health Career Opportunity Programs; and UConn Health.